

**B.TECH. DEGREE EXAMINATION, DECEMBER 2012****Third Semester**

Branch : Computer Science/Information Technology

EN 010 301 B—ENGINEERING MATHEMATICS-II (CS, IT)

(New Scheme—Regular/Improvement/Supplementary)

Time : Three Hours

Maximum : 100 Marks

**Part A***Answer all questions briefly.  
Each question carries 3 marks.*

- Write in symbolic form :
  - All the world loves a lover.
  - It is not true that London is in India.
  - It is false that  $7 + 6 = 13$  and  $5 + 5 = 7$ .
- Differentiate between one-to-one and onto functions.
- Define equivalence relation.
- Let  $A$  be any subset of the real number system  $R$  with the usual order. Under what conditions is  $A$  a lattice ?
- Draw a diagram for the graph  $G = G(V, E)$ ,  $V = \{A, B, C, D\}$ ,  $E = \{\{A, B\}, \{D, A\}, \{C, A\}, \{C, D\}\}$ .

**Part B**

(5 × 3 = 15 marks)

*Answer all questions.  
Each question carries 5 marks.*

- State and explain duality law. Write the dual of  $\neg(P \vee Q) \wedge (P \vee \neg(Q \wedge \neg S))$ .
- The functions  $f: A \rightarrow B$ ,  $g: B \rightarrow C$  and  $h: C \rightarrow D$ . Prove that  $h \circ (g \circ f) = (h \circ g) \circ f$ .
- Suppose  $R$  and  $S$  are transitive relations on a set  $A$ . Show that  $R \cap S$  is also transitive.
- Consider the power set  $P(A)$  of  $A = \{a, b, c\}$  which is a bounded lattice under the operations of intersection and union. Find the complement of  $X = \{a, b\}$  if it exists.
- Draw a diagram of the following directed graph  $G$  where  $V(G) = \{A, B, C, D, E\}$  and  $E(G) = \{\{A, D\}, \{B, C\}, \{C, E\}, \{D, B\}, \{D, D\}, \{D, E\}, \{E, A\}\}$ .

(5 × 5 = 25 marks)

## Part C

Answer any **one** full question from each module.  
Each full question carries 12 marks.

## Module 1

11. (a) Find the truth tables for :

(i)  $p \wedge (q \vee r)$  and

(ii)  $(p \wedge q) \vee (p \wedge r)$ .

(6 marks)

(b) Verify that the proposition  $p \vee \sim (p \wedge q)$  is a tautology.

(6 marks)

Or

12. (a) Negate the following :

(i)  $\forall x \exists y (p(x) \vee q(y))$ .

(ii)  $\exists x \forall y (p(x, y) \rightarrow q(x, y))$ .

(6 marks)

(b) Let  $A = \{1, 2, 3, 4\}$  be the universal set. Determine the truth value of each statement :

(i)  $\forall x, x+3 < 6$ .

(ii)  $\exists x, x+3 < 6$ ,

(iii)  $\exists x, 2x^2 + x = 15$ .

(6 marks)

## Module 2

13. (a) Suppose  $f : A \rightarrow B$  and  $g : B \rightarrow C$  are into functions. Show that  $g \circ f : A \rightarrow C$  is an onto function.

(6 marks)

(b) Solve each of the following linear congruence equations :

(i)  $3x \equiv 2 \pmod{8}$ .

(ii)  $6x \equiv 5 \pmod{9}$ .

(iii)  $4x \equiv 6 \pmod{10}$ .

(6 marks)

Or

14. (a) State and explain Euclidean algorithm. Use it to find the gcd of 1052 and 356.\* (6 marks)

(b) Using Pigeonhole principle show that the decimal expansion of a rational number, must, after some point, become periodic.

(6 marks)

## Module 3

15. (a) Let  $A = \{1, 2, 3, \dots, 13, 14, 15\}$ . Let  $R$  be the relation on  $A$  defined by congruence modulo 4. Find the equivalence classes determined by  $R$ .

(6 marks)

- (b) Determine whether or not each of the following is a partition of the set  $N$  of positive integers :

(i)  $\{\{n : n > 5\}, \{n : n < 5\}\}$ .

(ii)  $\{\{n : n > 5\}, \{0\}, \{1, 2, 3, 4, 5\}\}$ .

(iii)  $\{\{n : n^2 > 11\}, \{n : n^2 < 11\}\}$ .

(6 marks)

Or

16. (a) Suppose  $R$  and  $S$  are reflexive relations on a set  $A$ . Show that  $R \cap S$  is reflexive. (6 marks)

- (b) Give examples of relations  $R$  on  $A = \{1, 2, 3\}$  having the stated property :

(i)  $R$  is both symmetric and antisymmetric.

(ii)  $R$  is neither symmetric nor antisymmetric.

(iii)  $R$  is transitive but  $R \cup R'$  is not transitive.

(6 marks)

## Module 4

17. (a) Let  $C$  be a collection of sets which are closed under intersection and union. Verify that  $(C, \cap, \cup)$  is a lattice.

(6 marks)

- (b) Consider the power set  $P(A)$  of  $A = \{a, b, c\}$  which is a bounded lattice under the operations of intersection and union. Find the complement of  $X = \{a, b\}$  if it exists.

(6 marks)

Or

18. (a) Suppose  $L$  is a bounded lattice with lower bound  $O$  and upper bound  $I$ . Show that  $O$  and  $I$  are complements of each other.

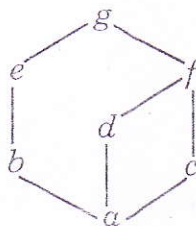
(6 marks)

- (b) Consider the lattice  $M$  in the figure shown below :

(i) Find the nonzero join-irreducible elements and the atoms of  $M$ .

(ii) Is  $M$  distributive ?

(6 marks)



Turn over



## Module 5

19. (a) Let  $a$ ,  $b$  and  $c$  be three distinct vertices in a graph. There is a path between  $a$  and  $b$  and also there is a path between  $b$  and  $c$ . Prove that there is a path between  $a$  and  $c$ .

(6 marks)

- (b) Prove that any two simple connected graphs with  $n$  vertices, all of degree two, are isomorphic.

(6 marks)

Or

20. (a) Show a tree in which its diameter is not equal to twice the radius. Under what condition does this inequality hold? Elaborate.

(6 marks)

- (b) Prove that a pendant edge (an edge whose one end vertex is of degree one) in a connected graph  $G$  is contained in every spanning tree of  $G$ .

(6 marks)

[5 × 12 = 60 marks]